

HYPHEN: A multi-thruster simulation platform

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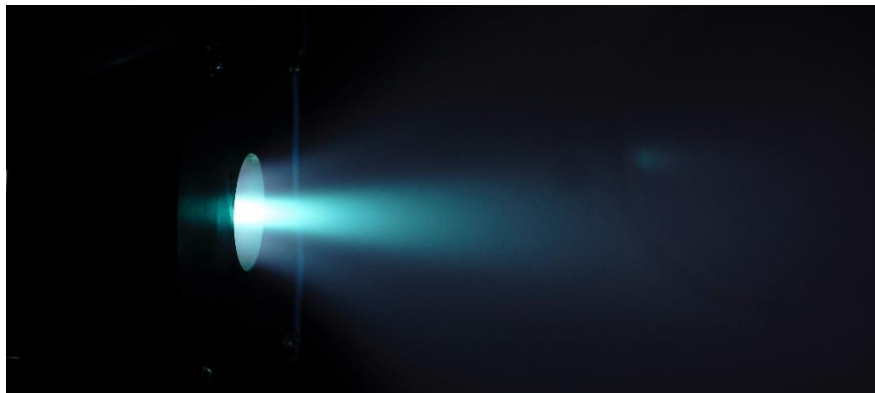
*Plasmas and Space Propulsion Team
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Plasmas and Space Propulsion Team (EP2)

- ~20 year R&D experience
 - Modeling
 - Code development
 - Testing (since 2016)
- ~15 Researchers
- ~ 40 R&D projects
 - FP7 and H2020
 - ESA, US-AFOSR
 - National R&D Plans
- ~60+120 papers, 1 patent
- Large background in teaching EP physics
- Large experience in international & industrial collaborations

- ❑ Modeling and simulation
 - Hall-effect thrusters
 - Electrodeless thrusters (HPT, ECRT)
 - Propulsive magnetic nozzles
 - Hollow cathodes, AF-MPDT (incipient)
 - Plasma plume characterization (unmagnetized & magnetized)
 - Contactless Debris Removal & Plume-Spacecraft interaction
 - Electrodynamic Tethers
 - Plasma-surface interaction
 - Plasma instabilities and turbulence
- ❑ Plasma diagnosis (theory & design)
- ❑ Thruster design, development, testing

EP2 vacuum facility



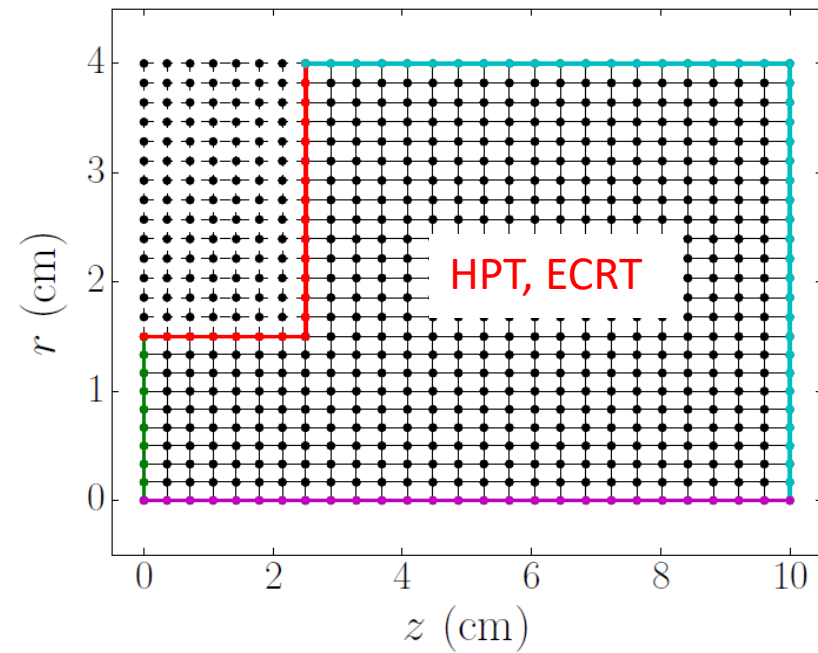
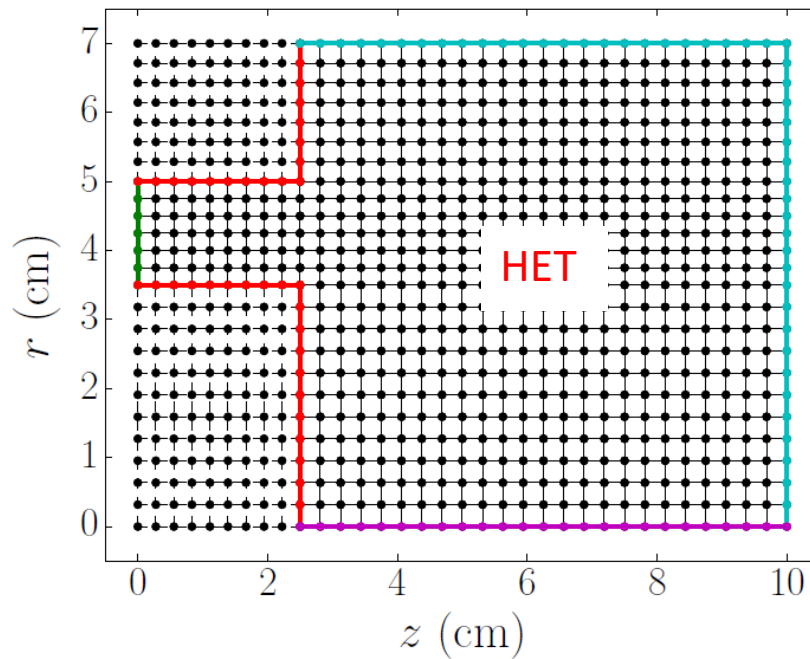
HYPHEN: A multi-thruster simulator

- Project to be developed along 2019
- Multi-thruster simulation platform for electromagnetic thrusters (EMT) operating with rarefied (i.e. weakly-collisional) plasmas
 - ❑ EMT with electrodes: HET, HEMPT, AF-MPDT
 - ❑ EMT with EM emission: HPT, ECRT, VASIMR
- From converging ongoing EP2 developments for individual thrusters:
 - ❑ NOMADS within H2020-CHEOPS
 - ❑ SURFET within H2020-MINOTOR
 - ❑ HELPIC within AirbusDS (F) funded project
- Improves thruster physics understanding, optimize code development
- Axisymmetric (2D), hybrid (PIC-MC/fluid), modular, OMP-parallelized
- HYPHEN will share structure and algorithms with EP2PLUS (3D hybrid code, focused on plumes)
 - ❖ EP2PLUS presentation on Wednesday 17 at 5:30 PM
- HYPHEN will include our Magnetic Nozzle Physics models
 - ❖ Magnetic Nozzles presentation on Wednesday 17 at 2:00 PM

Code modular structure

- **Ion-module**
 - ❑ PIC-MC, multi-species
- **Electron-module**
 - ❑ Highly-magnetized, weakly-collisional fluid
 - ❑ Will include pressure anisotropy & magnetic mirror effects
 - ❑ Needs turbulent transport models !
 - ❑ Auxiliary full-PIC code will provide 'kinetic' information
- **Wave-module** (only for electrodeless HPT, ECRT,...)
 - ❑ Maxwell eqs + dielectric tensor → strong coupling with E-module
 - ❑ Provides heating and other wave effects to E-module
- **Sheath-module**
 - ❑ By default plasma is quasineutral (but Poisson solver can be added)
 - ❑ Admits different wall types (dielectric, metallic, emissive,...)
- **Circuit-module**
 - ❑ Essential in HPT, ECRT for overall performance calculation
 - ❑ Simplifies numerical convergence when different wall-types are present

Ion Module



- Operates on a **structured mesh** (ad-hoc PIC mesh generator)
- Possibility of including **inner active surfaces** (conducting or dielectric walls)
- 3D Cartesian particle mover: provides accuracy **symmetry axis**
- **Improved PIC statistics:**
 - ❑ **Independent multiple populations**
 - ❑ Generation weight-based **population control**
 - ❑ **Cylindrical corrections**

Electron Module

Continuity & Momentum Eqs.

$$\nabla \cdot (\mathbf{j}_e + \mathbf{j}_i) = I_d$$

$$\mathbf{j}_e = \mathcal{K}_\sigma \cdot \left(-\nabla\phi + \frac{1}{en_e} \nabla p_e - \sum_Z \eta_{iZ} \mathbf{j}_{iZ} \right)$$

$$\mathcal{K}_\sigma = \begin{bmatrix} \sigma_\top & -\sigma_H & 0 \\ \sigma_H & \sigma_\top & 0 \\ 0 & 0 & \sigma_\parallel \end{bmatrix} \quad \sigma_\parallel = \frac{e^2 n}{m_e v_e} \quad \sigma_H = \chi_e \sigma_\top$$

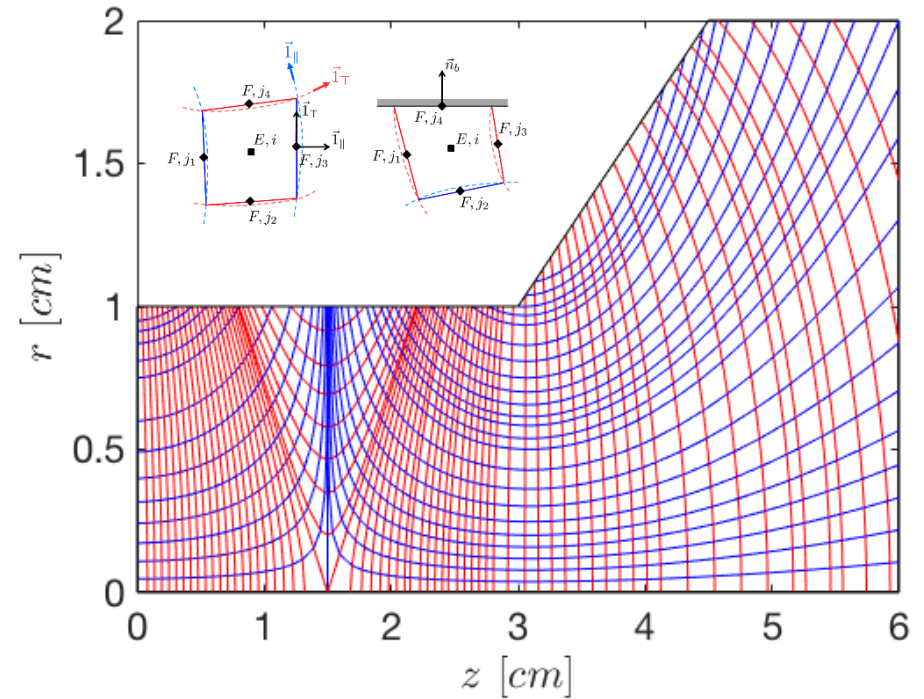
$$\sigma_\top = \frac{\sigma_\parallel}{1 + \chi_e^2} \quad \chi_e = \frac{\omega_{ce}}{v_e}$$

Internal Energy & Heat Flux Eqs.

$$\frac{\partial}{\partial t} \left(\frac{3}{2} p_e \right) - \nabla \cdot \left(\frac{3}{2} p_e \frac{\mathbf{j}_e}{en_e} \right) - p_e \nabla \cdot \left(\frac{\mathbf{j}_e}{en_e} \right) + \nabla \cdot \mathbf{q}_e =$$

$$E_{coll} + \frac{\mathbf{j}_e}{en_e} \cdot \left(\mathbf{M}' - \frac{\mathbf{j}_e}{2en_e} m_e S_e \right) + Q_a$$

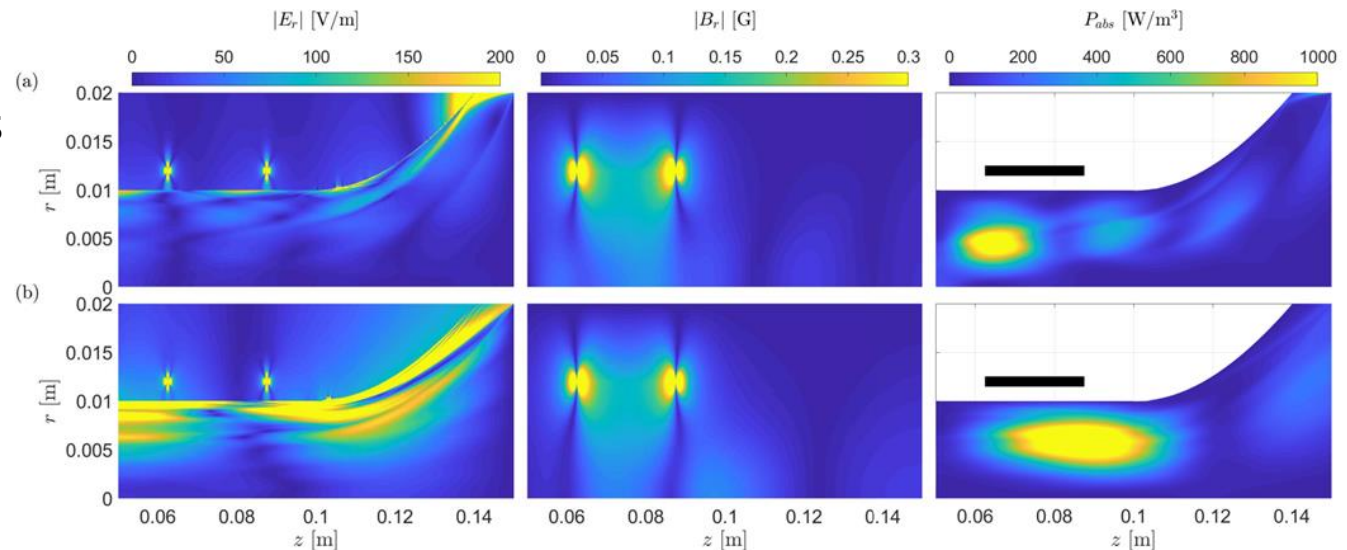
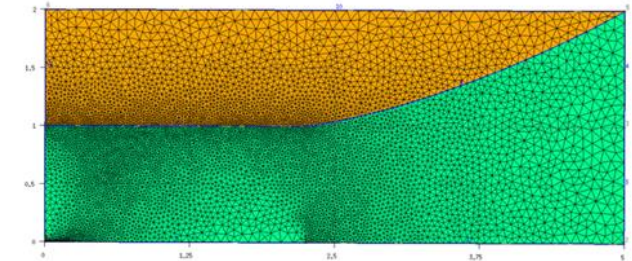
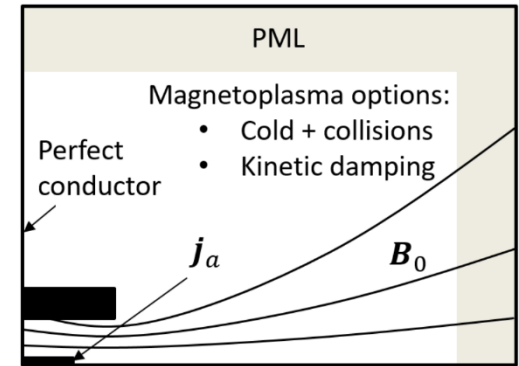
$$\frac{5}{2} p_e \nabla \cdot \left(\frac{\mathbf{j}_e}{m_e n_e} \right) + \omega_{ce} (\mathbf{q}_e \wedge \mathbf{l}_\parallel) = \mathbf{H}_{coll} - \frac{5}{2} \frac{p_e}{m_e n_e} \mathbf{M}'$$



- Finite volume method on Magnetic Field Aligned Mesh
- Limits impact of numerical diffusion.
- Very irregular cells, specially at boundaries and null points
- Accuracy issues

Wave Module

- Wave-plasma interaction module for HPTs, ECRTs provides
 - ❑ wavefields,
 - ❑ power deposition maps
 - ❑ plasma impedance
- Maxwell eqs. + dielectric tensor in the ω -domain
 - ❑ HPT: Finite Differences
 - ❑ ECRT (MINOTOR): Finite Elements
- Severe numerical difficulties
 - ❑ Numerical dispersion
 - ❑ Resonances
 - ❑ Short wavelengths
- Perfectly matched layers for radiation to free space

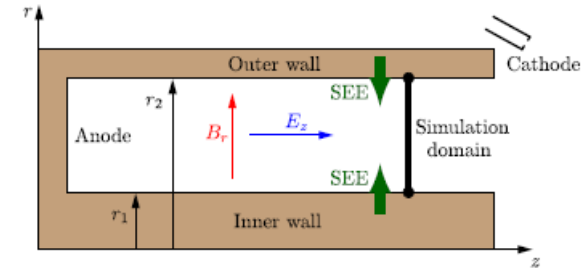


2D wavefields and absorbed power maps in a HPT under two operating conditions

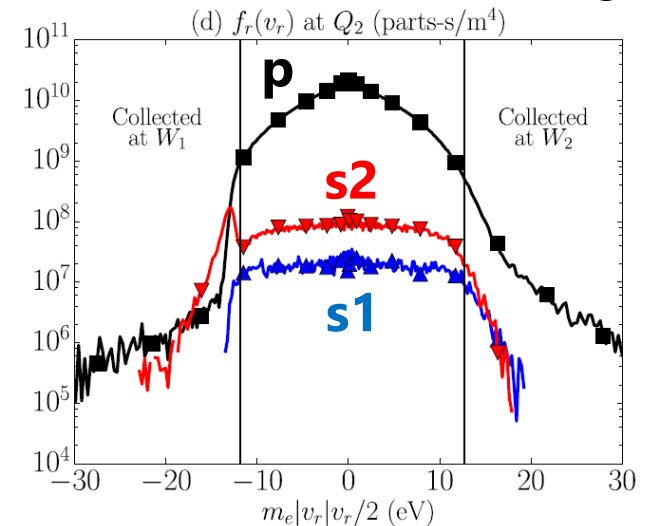
Auxiliary full-PIC code for EVDF

1D radial full-PIC code for HET

- Study of electron VDFs with strong wall SEE
- T-anisotropy → magnetic mirror effects
- Primary and secondary electrons behave differently
- SEE is partially thermalized, partially recollected
- Cylindrical effects are significant
- Information on macroscopic magnitudes and eqs.
 - ❑ Correction to Boltzmann-Maxwell equilibrium
 - ❖ Up to 30% in our simulations
 - ❑ Correction factors to energy fluxes to the wall
 - ❑ Ways to include SEE in single-fluid equations



EVDFs at outer wall sheath edge



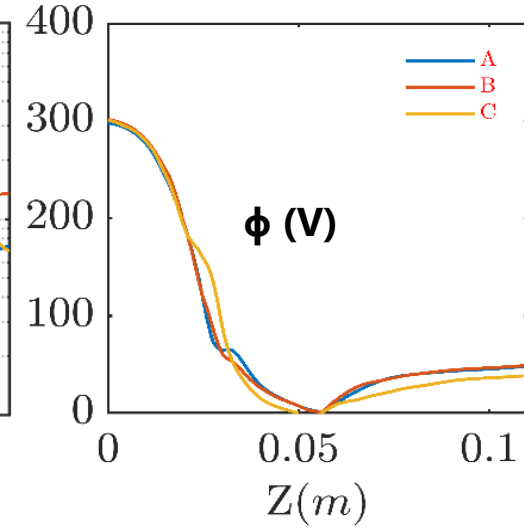
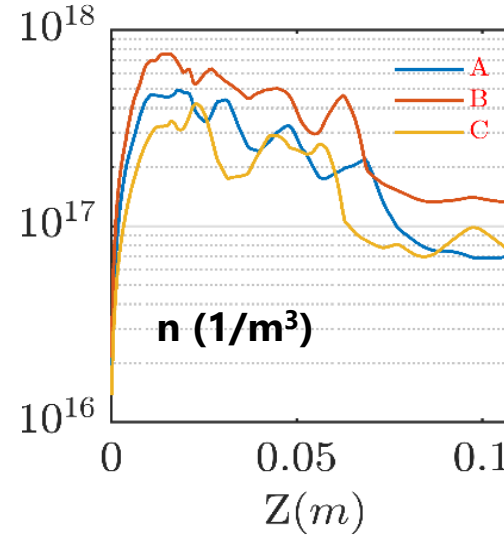
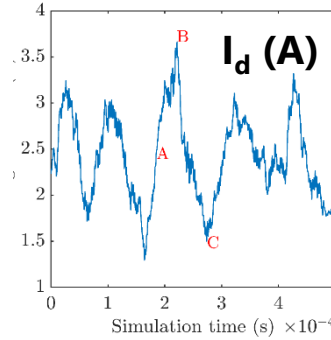
$$\underbrace{e\phi - e\phi_M - T_{rpM} \ln \frac{n_p}{n_{pM}}}_{\text{Boltzmann relation terms}} = \underbrace{\left[T_{rp} - T_{rpM} + \int_{r_M}^r dr (T_{rp} - T_{rpM}) \frac{d \ln n_p}{dr} \right]}_{\text{Non-uniform radial temperature}} + \underbrace{\int_{r_M}^r dr \frac{T_{rp} - T_{\perp p}}{r}}_{\text{T-anisotropy + magnetic mirror}} - \underbrace{\int_{r_M}^r dr \frac{m_e u_{\theta p}^2}{r}}_{\text{Centrifugal force}}$$

Results for CHEOPS

Base SPT-100 configuration

PPU control	V_d	\dot{m} (Xe)	PIC Δt	NOMADS Δt
Constant voltage	300V	$5 \frac{mg}{s}$	$10^{-8}s$	$10^{-10}s$

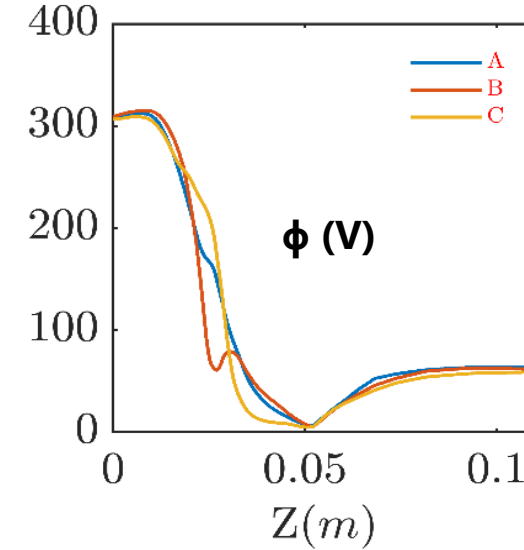
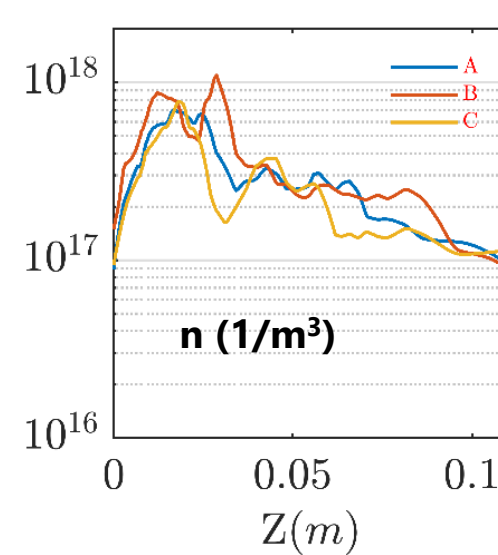
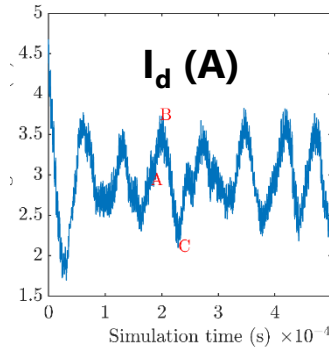
No. PIC mesh elements	1080
Avg. No. macroparticles	$\sim 10^5$ Neutrals, $\sim 9 \times 10^4$ Single Ions, $\sim 9 \times 10^4$ Double Ions
No. MFAM elements	1326
No. cores	20
Computation time	$7.17 \times 10^4 s (\sim 20h)$: $4.6 \times 10^3 s$ in PIC, $6.6 \times 10^4 s$ in NOMADS



Singular SPT-100 configuration

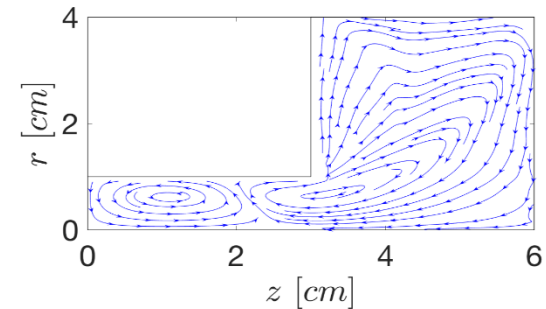
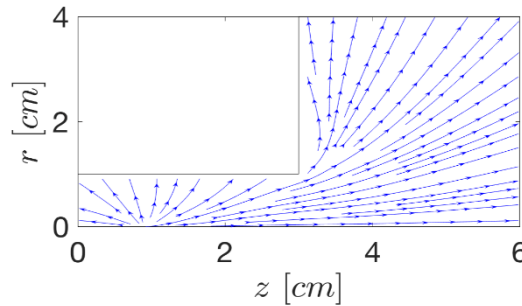
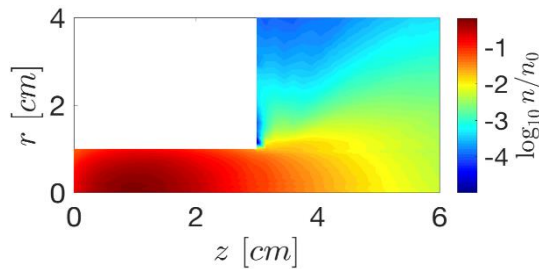
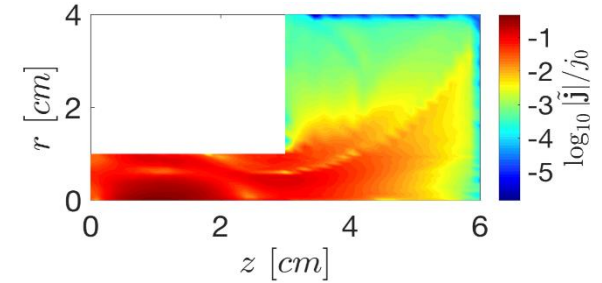
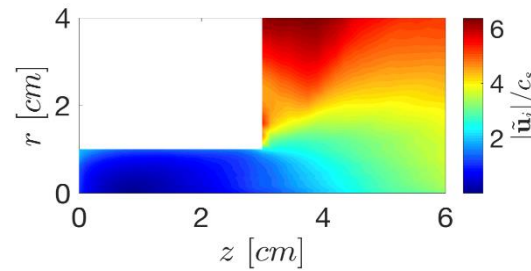
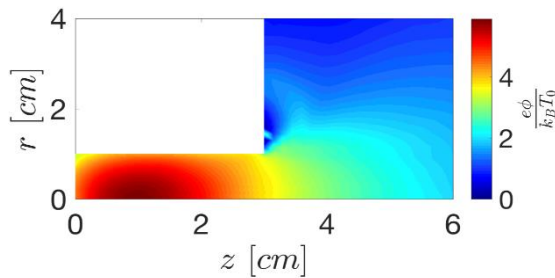
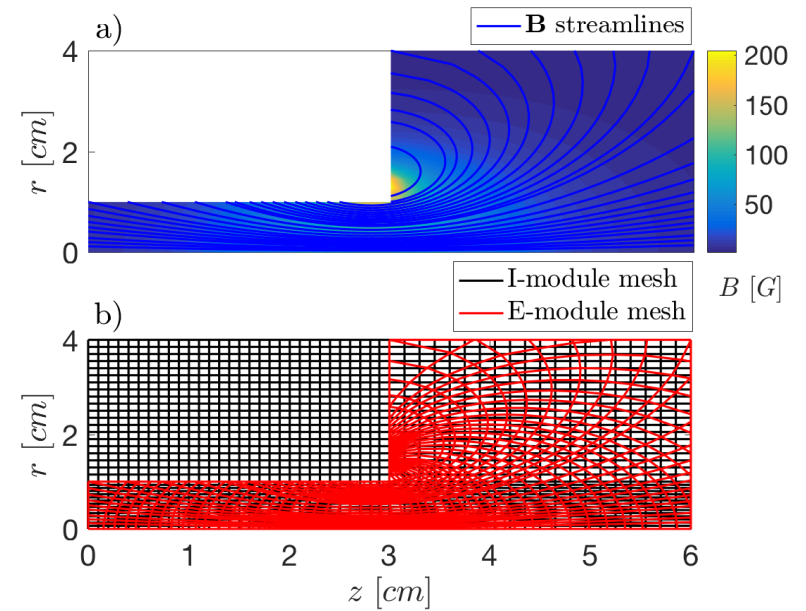
PPU control	V_d	\dot{m} (Xe)	PIC Δt	NOMADS Δt
Constant voltage	300V	$5 \frac{mg}{s}$	$10^{-8}s$	$10^{-10}s$

No. PIC mesh elements	1080
Avg. No. macroparticles	$\sim 10^5$ Neutrals, $\sim 7 \times 10^4$ Single Ions, $\sim 7 \times 10^4$ Double Ions
No. MFAM elements	2453
No. cores	20
Computation time	$18.8 \times 10^4 s (\sim 50h)$: $4.0 \times 10^3 s$ in PIC, $18.4 \times 10^4 s$ in NOMADS



Results for HPT

- Partial results without Wave module
- Simulation here for $T_e \propto n_e^{\gamma-1}$
- In progress: simulation with prescribed map of energy deposition
- Adaptation to ECRT (MINOTOR) in progress

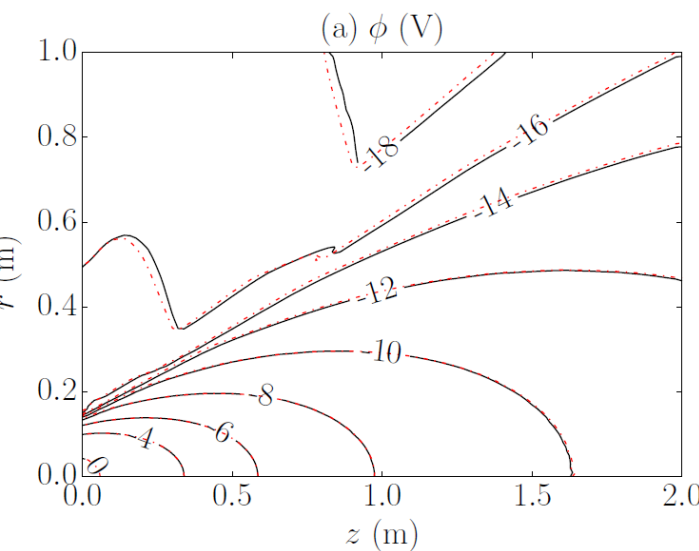


Benchmarking 2Dcyl and 3D codes

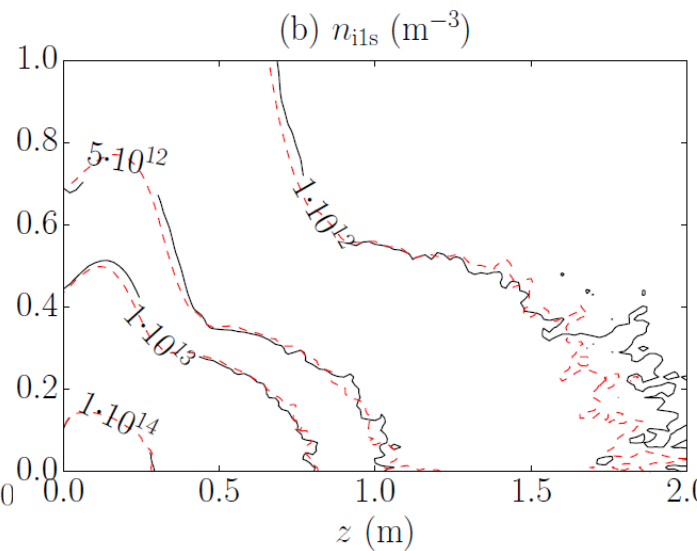
- Excellent agreement between 2Dcyl NOMADS and 3D EP2PLUS
 - ❑ Electron module reduced to polytropic electron closure
 - ❑ 6 heavy species treated separately
 - ❑ Weighting more complex in 2D
- Comparable noise level: typical ten-times computational cost gain in 2D
- CEX ions: generated in near plume, accelerated sideways of plume core
 - ❑ Characterization of their density & energy (for S/C sputtering, ...)

Total N. parts. 2D	6.5M
Total N. parts. 3D	143M

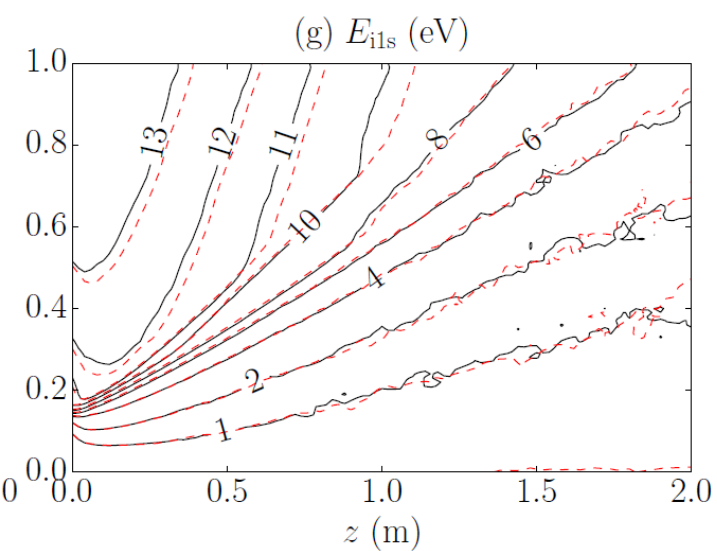
Electric potential



Slow singly-charged ions density



Slow singly-charged ions energy



Thank you! Questions?

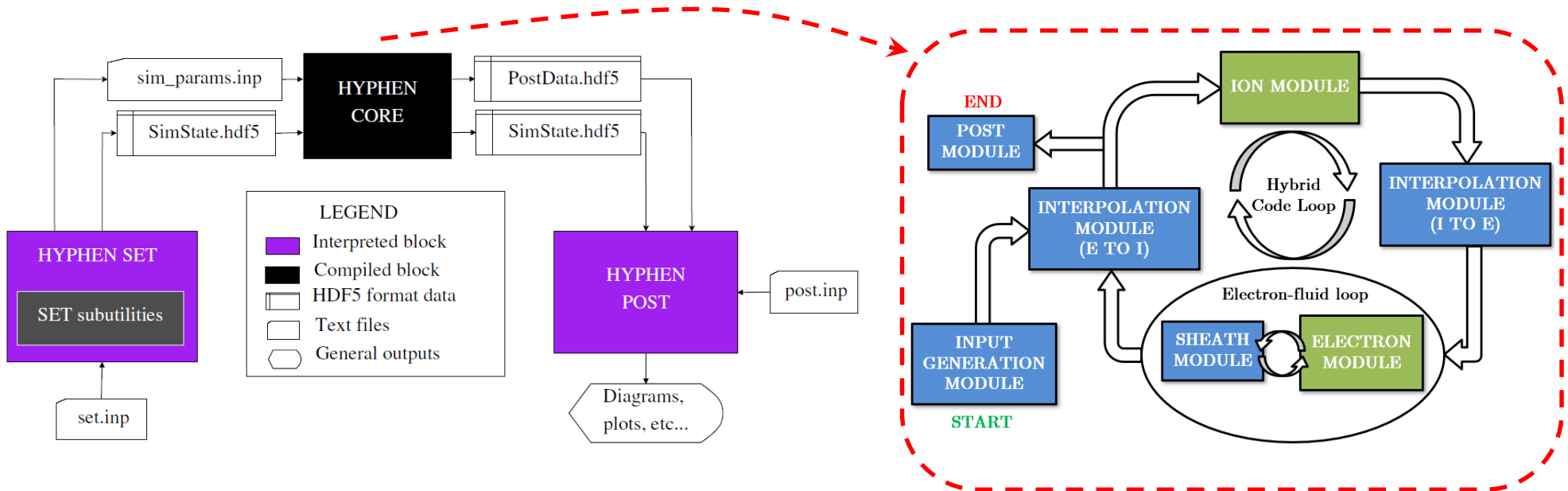


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Code structure

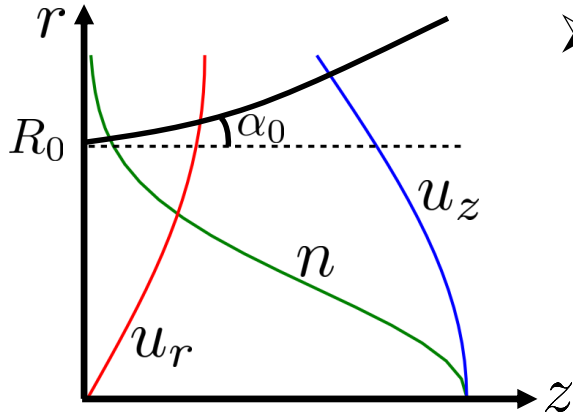


➤ 3 INDEPENDENT UNITS:

- ❑ SET: Pre-processing tasks (Python/Matlab)
- ❑ CORE: Main simulation tasks (Fortran)
- ❑ POST: Post-processing tasks (Python/Matlab)
- HDF5 for I/O data management

- Open-MP parallelization
- Test Driven Design (TDD) development philosophy
- Version control through a Mercurial online repository

Benchmarking 2D and 3D codes



Ions injection: Generalized Parks-Katz SSM profiles (Parks & Katz, 1979, Merino et al 2015)

$$R_0 = 14 \text{ cm}, \gamma = 1.2$$

➤ NASA's NSTAR GIT plume simulation (Brophy 2002):

- ❑ 3D simulation domain: 2m side cubic
- ❑ 2D simulation domain: cylinder 1m radius 2m long
- ❑ Circular injection area with radius $R = 14 \text{ cm}$

N. cells 3D	-	$4 \cdot 10^6$
N. cells 2D	-	$1 \cdot 10^4$
$\Delta x = \Delta y \equiv \Delta r, \Delta z$	cm	1, 2
Δt , N. steps, Sim. time	s, N/A, ms	$3 \cdot 10^{-7}$, $5 \cdot 10^4$, 15
T_{e0}, γ	eV, -	3.5, 1.2

Population	Type	Origin
$i1s$	Xe ⁺ Slow	Ionization and CEX 0 → 1 collisions
$i1f$	Xe ⁺ Fast	Injected SSM: $\alpha_0 = 20.5 \text{ deg}$, $T = 0.1 \text{ eV}$
$i2s$	Xe ⁺⁺ Slow	Ionization 0 → 2 and 1 → 2 and CEX 0 → 2 collisions
$i2f$	Xe ⁺⁺ Fast	Injected SSM: $\alpha_0 = 30 \text{ deg}$, $T = 0.2 \text{ eV}$
ns	Xe Slow	Injected flat profile: sonic conditions at $T = 0.05 \text{ eV}$
nf	Xe Fast	CEX 0 → 1 and 0 → 2 collisions